

Heisenberg's Uncertainty Principle:-

(18)

This Principle was discovered by Heisenberg in 1927. It states that we can measure either position or momentum of a particle with any desired degree of accuracy (within limit of experimental equipment). OR

It is impossible to measure both, position and momentum simultaneously with accuracy.

$$\Delta x \cdot \Delta p_x \geq \frac{h}{4\pi}$$

$\Delta x \rightarrow$ Uncertainty in position.

$\Delta p \rightarrow$ Uncertainty in momentum.

Physical Significance!

- I) Uncertainty Principle explain why it is possible for radiation and matter to have dual (wave-particle) character.
- II) It also make it clear that we can predict only the probable behaviour of quantum mechanical system not the exact behaviour.
- III) It helps in understanding many phenomenon like absence of electron within nuclei, natural broadening of spectral lines etc.

Energy Momentum Uncertainty!

The uncertainty relation for simultaneous measurement of Energy E & time t expressed as.

$$\Delta E \cdot \Delta t \geq \frac{\hbar}{2} \quad \left(\hbar = \frac{h}{2\pi} \right)$$

Derivation let us consider a microparticle moving with velocity v , Its kinetic Energy will be -

$$E = \frac{1}{2} m v^2$$

$$\Delta E = \Delta \left(\frac{1}{2} m v^2 \right)$$

$$= m v \Delta v = v \Delta p$$

$$\left(v^2 \frac{\Delta k}{\Delta t} \right)$$

$$\Rightarrow \Delta E = \frac{\Delta k}{\Delta t} \Delta p$$

$$\Delta E \cdot \Delta t = \Delta k \cdot \Delta p$$

$$\Delta E \cdot \Delta t \geq \frac{\hbar}{2}$$

$$\Delta k \cdot \Delta p \geq \frac{\hbar}{2}$$